Optical and Other Measurement Techniques of Carrier Lifetime in Semiconductors

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Abstract In this paper, various methods for characterization of semiconductor charge carrier lifetime are reviewed and an optical technique is described in detail. This technique is contactless, all-optical and based upon measurements of free carrier absorption transients by an infrared probe beam following electron-hole pair excitation by a pulsed laser beam. Main features are a direct probing of the excess carrier density coupled with a homogeneous carrier distribution within the sample, enabling precision studies of different recombination mechanisms. The method is capable of measuring the lifetime over a broad range of injections (10^{13}-10^{18} \text{ cm}^{-3}) probing the minority carrier lifetime, the high injection lifetime and Auger recombination, as well as the transition between these ranges. Performance and limitations of the technique, such as lateral resolution, are addressed while application of the technique for lifetime mapping and effects of surface recombination are also outlined.

Results from detailed studies of the injection dependence yield good agreement with the Shockley–Read–Hall theory, whereas the coefficient for Auger recombination shows an apparent shift to a higher value, with respect to the traditionally accepted value, at carrier densities below 2 \times 10^{17} \text{ cm}^{-3}. Data also indicate an increased value of the coefficient for bimolecular recombination from the generally accepted value. Measurement on an electron irradiated wafer and wafers of exceptionally high carrier lifetimes are also discussed within the framework of different recombination mechanisms.

Keywords Carrier Lifetime, Electron-Hole Pair, Shockley–Read–Hall Recombination, Generation

1. Introduction

With the decrease in feature size in semiconductor manufacturing, molecular contamination problems are increased significantly[1]. Recombination lifetime as well as diffusion length measurements have become ubiquitous in the semiconductor industry, because they are a good indicator of wafer contamination[2]. When the defect densities in semiconductors are low, lifetime is one of few parameters that gives significant information about the lower concentration. No other technique can detect defect densities as low as 10^{9}–10^{11} \text{ cm}^{-3} in a simple, contactless room temperature measurement. In principle, there is no lower limit to the defect density determined by lifetime measurements[3]. It is for these reasons that the IC industry, largely concerned with unipolar MOS devices in which lifetime plays a minor role, has adopted lifetime measurements as a “process cleanliness monitor”[4]. Alongside this, recombination and generation lifetime as well as measurements of carrier diffusion lengths in semiconductors are also very crucial for photovoltaic devices[5] which have recently become very attractive topic to researchers.

The theory of electron-hole pair recombination through recombination centers (traps) was put forth in 50s of the last century in the well-known works by Shockley-Read-Hall (SRH)[6,7]. Here, we discuss lifetimes, their dependence on semiconductor material and device parameters like energy level, injection level & surfaces and how lifetimes are measured. Different measurement methods can give widely differing lifetimes for the same material or device. In most cases, the reasons for these discrepancies are fundamental and are not due to a deficiency of the measurement. The difficulty with defining a lifetime is that we are describing a property of a carrier within the semiconductor rather than the property of the semiconductor itself.

2. Theory

There are two principal categories of carrier lifetimes: recombination lifetimes and generation lifetimes. The concept of recombination lifetime \( \tau_r \) holds when excess carriers decay as a result of recombination. Generation lifetime \( \tau_g \) applies when there is a paucity of carriers, as in the space-charge region of a reverse-biased device and the device tries to attain equilibrium. During recombination an electron-hole pair ceases to exist on average after a time \( \tau_r \), illustrated in Fig. 1(a). The generation lifetime, by analogy, is the time that it takes on average to generate an ehp, illustrated in Fig. 1(b). Thus generation lifetime is a misnomer, since the creation of
an ehp is measured and generation time would be more appropriate. Nevertheless, the term “generation lifetime” is commonly accepted. When these recombination and generation events occur in the bulk, they are characterized by $\tau_r$ and $\tau_g$. When they occur at the surface, they are characterized by the surface recombination velocity $s_r$ and the surface generation velocity $s_g$, also illustrated in Fig. 1. Both bulk and surface recombination or generation occur simultaneously and their separation is sometimes quite difficult. Consisting of bulk and surface components, the measured lifetimes are always effective lifetimes.

It is instructive to consider $\tau_r$ and $\tau_g$ in more detail before discussing lifetime measurement techniques. The excess ehps may have been generated by photons or particles of energy higher than the band gap or by forward biasing a $pn$ junction. There are more carriers after the stimulus than before and the excess carriers return to equilibrium by recombination.

Figure 1. Illustration of various recombination and generation mechanisms for a (a) forward-biased and (b) reverse-biased junction

2.1. Recombination Lifetime and Surface Velocity

The departure of the carrier densities from their equilibrium values non-linearly controls the bulk recombination rate $R$. We consider a p-type semiconductor throughout this work and are chiefly concerned with the behavior of the minority electrons. Confining ourselves to linear, quadratic, and third order terms, $R$ can be written as

$$ R = A(n - n_o) + B(p - p_o) + C_s \left(p^{n_o}n - p_o^n n_o\right) + C_g \left(p n^2 - p_o n_o^2\right) $$

(1)

where $n = n_o + \Delta n$, $p = p_o + \Delta p$, $n_o$, $p_o$ are the equilibrium and $\Delta n$, $\Delta p$, the excess carrier densities. In the absence of trapping, $\Delta n = \Delta p$, allowing Eq. (1) to be simplified to

$$ R = A\Delta n + B \left(p_o + \Delta n\right) + C_s \left(p_o^{n_o} + 2p_o \Delta n + \Delta n^2\right) + C_g \left(n_o^2 + 2n_o \Delta n + \Delta n^2\right) $$

(2)

where some terms containing $n_o$ have been dropped because $n_o \ll p_o$ in a p-type material. The recombination lifetime is defined as

$$ \tau_r = \frac{\Delta n}{R} $$

(3a)

giving

$$ \frac{1}{\tau_r} = A + B \left(p_o + \Delta n\right) + C_s \left(p_o^{n_o} + 2p_o \Delta n + \Delta n^2\right) + C_g \left(n_o^2 + 2n_o \Delta n + \Delta n^2\right) $$

(3b)

There are three main recombination mechanisms those determine the recombination lifetime: SRH or multiphonon recombination characterized by $\tau_{SRH}$, radiative recombination characterized by $\tau_{rad}$ and Auger recombination characterized by $\tau_{Auger}$. These mechanisms are illustrated in Fig. 2.

The recombination lifetime $\tau_r$ is determined according to the relationship given below

$$ \tau_r = \frac{1}{\tau_{SRH}^{-1} + \tau_{rad}^{-1} + \tau_{Auger}^{-1}} $$

(4)

1) SRH Recombination: During SRH recombination, ehp's recombine through deep-level impurities or traps, characterized by the density $N_T$, energy level $E_T$ and capture cross-sections $\sigma_p$ and $\sigma_n$ for electrons and holes, respectively. The energy liberated during the recombination event is dissipated by lattice vibrations or phonons, illustrated in Fig. 2(a). The SRH lifetime is given by[6]

$$ \tau_{SRH} = \tau_r \left(n_o + n + \Delta n\right) + \tau_r \left(p_o + p + \Delta p\right) $$

(5)

where $n_1$, $p_1$, $\tau_n$ and $\tau_p$ are defined as

$$ n_1 = n_o \exp\left(\frac{E_T - E_c}{kT}\right) $$

(6a)

$$ p_1 = n_o \exp\left(\frac{E_T - E_v}{kT}\right) $$

(6b)

2) Radiative Recombination: During this recombination, ehp's recombine directly from band to band with the energy carried away by photons as shown in Fig. 2(b). The radiative lifetime is[8]

$$ \tau_{rad} = \frac{1}{B \left(p_o + n_o + \Delta n\right)} $$

(7)

B is the radiative recombination coefficient. The radiative lifetime is inversely proportional to the carrier density because in band-to-band recombination both electrons and holes must be present simultaneously.

3) Auger Recombination: During Auger recombination, as illustrated in Fig. 2(c), the recombination energy is absorbed by a third carrier and the Auger lifetime is inversely proportional to the carrier density squared. The Auger lifetime is given by

$$ \tau_{Auger} = \frac{1}{C_p \left(p_o^2 + 2p_o \Delta n + \Delta n^2\right) + C_g \left(n_o^2 + 2n_o \Delta n + \Delta n^2\right)} $$

(8)

where $C_p$ is the Auger recombination coefficient for holes.
and \( C_n \) for electrons. Values for radiative and Auger coefficients are given in Table 1.

### Table 1. Recombination Coefficients

<table>
<thead>
<tr>
<th>Semiconductor</th>
<th>Temperature (K)</th>
<th>Radiative Recombination Coefficient, ( B ) (cm(^3)/s)</th>
<th>Auger Recombination Coefficient, ( C_n ) (cm(^3)/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Si</td>
<td>300</td>
<td>( 4.73 \times 10^{-13} ) [10]</td>
<td>( C_n = 2.8 \times 10^{-30}, C_p = 10^{-30} ) [11 D/5]</td>
</tr>
<tr>
<td>Si</td>
<td>300</td>
<td>( 8.01 \times 10^{-14} ) [10]</td>
<td>( C_n = C_p = 2-35 \times 10^{-30} ) [11 B/G]</td>
</tr>
<tr>
<td>Si</td>
<td>77</td>
<td>( 5.2 \times 10^{-14} ) [5]</td>
<td>( C_n = 8 \times 10^{-35}, C_p = 2.8 \times 10^{-31} )</td>
</tr>
<tr>
<td>Ge</td>
<td>300</td>
<td>( 1.7 \times 10^{-30} ) [8, 8/R]</td>
<td>( C_n = 1.6 \times 10^{-35}, C_p = 4.6 \times 10^{-35} ) [6]</td>
</tr>
<tr>
<td>GaAs</td>
<td>300</td>
<td>( 1.3 \times 10^{-30} ) [8, 8/R]</td>
<td>( C_n = 5 \times 10^{-36}, C_p = 2 \times 10^{-36} ) [8, 8/R]</td>
</tr>
<tr>
<td>GaP</td>
<td>300</td>
<td>( 5.4 \times 10^{-14} ) [5]</td>
<td>( C_n = 8 \times 10^{-35} )</td>
</tr>
<tr>
<td>InP</td>
<td>300</td>
<td>( 1.6 \times 10^{-14} ) [7]</td>
<td>( C_n = 3.7 \times 10^{-35}, C_p = 8.7 \times 10^{-36} ) [6]</td>
</tr>
<tr>
<td>InSb</td>
<td>300</td>
<td>( 4.4 \times 10^{-15} ) [5]</td>
<td>( C_n = C_p = 8 \times 10^{-39} ) [9]</td>
</tr>
</tbody>
</table>

#### 2.2. Recombination Lifetime and Level of Injections

Equations (5) to (8) simplify for both low-level and high-level injection. Low-level injection holds when the excess minority carrier density is low compared to the equilibrium majority carrier density, \( \Delta n \ll p_o \). Similarly, high-level injection holds when \( \Delta n \gg p_o \). The injection level is important during lifetime measurements. The appropriate expressions for low-level (\( ll \)) and for high-level (\( hl \)) injection become

\[
\tau_{SRH}(ll) = \frac{n_1}{p_o} \tau_p + \left(1 + \frac{P_r}{P_p}\right) \tau_s \approx \tau_s \tag{9}
\]

\[
\tau_{SRH}(hl) \approx \tau_p + \tau_s \tag{9a}
\]

where the second approximation in the \( \tau_{SRH}(ll) \) expression holds when \( n_1 \ll p_o \) and \( p_1 \ll p_o \).

\[
\tau_{rad}(ll) = \frac{1}{BP_n} \; ; \; \tau_{rad}(hl) = \frac{1}{B\Delta n} \tag{10}
\]

\[
\tau_{Auger}(ll) = \frac{1}{4\sigma p o} \; ; \; \tau_{Auger}(hl) = \frac{1}{4\sigma p o} \frac{(C_p + C_n)\Delta n^2}{\sigma n_s \sigma n_p \sigma p_s} \tag{11}
\]

The Si recombination lifetimes according to Eq. (4) are plotted in Fig. 3. At high carrier densities, the lifetime is controlled by Auger recombination and at low densities by SRH recombination. Auger recombination has the characteristic \( 1/n^2 \) dependence. The high carrier densities may be due to high doping densities or high excess carrier densities.

Whereas SRH recombination is controlled by the cleanliness of the material, Auger recombination is an intrinsic property of the semiconductor. Radiative recombination plays almost no role in Si except for very high lifetime substrates but is important in direct band gap semiconductors like GaAs.

The bulk SRH recombination rate is given by

\[
R = \frac{\sigma_n \sigma_p v_th N_i}{\sigma_i (n + n_i) + \sigma_p (p + p_i) + \tau_r (n + n_i) + \tau_a (p + p_i)} \tag{12}
\]

The surface SRH recombination rate is

\[
R_s = \frac{\sigma_n \sigma_p v_th N_i}{\sigma_s (n + n_s) + \sigma_p (p + p_s) + \tau_r (n + n_s) + \tau_a (p + p_s)} \tag{13}
\]

Where \( n_s = \sigma_u v_th N_i \); \( s_p = \sigma_p v_th N_i \). The subscript “s” refers to the appropriate quantity at the surface; \( n_s \) and \( n_i \) are the hole and electron densities (cm\(^{-3}\)) at the surface. The interface trap density \( N_t \) (cm\(^{-2}\)) is assumed constant in Eq. (13). If not constant, the interface trap density \( D_{it} \) (cm\(^{-2}\) eV\(^{-1}\)) must be integrated over energy with \( N_t \) in these equations given by \( N_t \approx kT D_{it} \) [9].

**Figure 3.** Recombination lifetime versus majority carrier density for n-Si with \( C_n = 2 \times 10^{-31} \) cm\(^3\)/s and \( B = 4.73 \times 10^{-15} \) cm\(^3\)/s.

**Figure 4.** Determination of bulk lifetime, surface recombination velocity and diffusion coefficient from lifetime measurements. Data from [10]
The surface recombination velocity $s_r$ is
\[ s_r = \frac{R}{\Delta n_i} \]  
from eq. (13)
\[ s_r = \frac{s_p n_s}{n_s (p_n + n_n + \Delta n_i) + s_p (p_n + p_p + \Delta p_i)} \]  
(14b)
The surface recombination velocity for low-level and high-level injection becomes
\[ s_r(I) = \frac{s_p n_s}{n_s (p_n/I_n + n_n + \Delta n_i) + s_p (p_n + p_p + \Delta p_i)} \approx s_r n_s \]  
(15)
$s_r$ depends strongly on injection level for the SiO$_2$/Si interface as shown in Fig. 4.

2.3. Recombination Lifetime Measurements Techniques
Recombination lifetime can be measured optically or electrically. The commonly used techniques are
1) Optical Measurements: Photoconduction Decay (PCD), Quasi-Steady-State Photoconduction (QSSPC), Short-Circuit Current/Open-Circuit Voltage Decay (SCCD/OCVD), Photoluminescence Decay (PLD), Surface Photovoltage (SPV), Steady-State Short-Circuit Current (SSSCC), Free Carrier Absorption, Electron Beam Induced Current (EBIC) etc.
2) Electrical Measurements: Diode Current-Voltage, Reverse Recovery (RR), Open-Circuit Voltage Decay (OCVD), Pulsed MOS Capacitor, Other Techniques.

3.1. Recombination Lifetime: Optical Measurements
Consider a $p$-type semiconductor with light incident on the sample. The light may be steady state or transient. The continuity equation for uniform ehp generation and zero surface recombination is [12,13]
\[ \frac{\partial \Delta n(t)}{\partial t} = G - R = \frac{\Delta n(t)}{\tau_{\text{eff}}} \]  
(20)
where $\Delta n(t)$ is the time dependent excess minority carrier density, $G$ the ehp generation rate and $\tau_{\text{eff}}$ the effective lifetime. Solving for $\tau_{\text{eff}}$ gives
\[ \tau_{\text{eff}}(\Delta n) = \frac{\Delta n(t)}{G(t) - d\Delta n(t)/dt} \]  
(21)
In the transient PCD method, with $G(t) < \ll d\Delta n(t)/dt$, the effective lifetime becomes $\tau_{\text{eff}}(\Delta n) = -\Delta n(t)/(d\Delta n(t)/dt)$. In the steady-state method, with $G(t) \gg d\Delta n(t)/dt$, the effective lifetime becomes $\tau_{\text{eff}}(\Delta n) = \Delta n/G$ and in the QSSPC method, Eq. (21) remains valid. Both $\Delta n$ and $G$ need to be known in the steady-state and QSSPC methods to determine the effective lifetime.
The excess carrier density decay for low level injection is given by

\[ \Delta n(t) = \Delta n(0) \exp \left( -\frac{t}{\tau_{\text{eff}}} \right) \]

where \( \tau_{\text{eff}} \) is calculated as

\[ \frac{1}{\tau_{\text{eff}}} = \frac{1}{\tau_a} + D \beta^2 \]  

(22)

with \( \beta \) found from the relationship \( \tan(\beta d/2) = s_r/(\beta D) \). Here \( \tau_a \) is the bulk recombination lifetime, \( D \) the minority carrier diffusion constant under low injection level and the ambipolar diffusion constant under high injection level and \( d \) the sample thickness. Equation (22) holds for any optical absorption depth provided the excess carrier density has ample time to distribute uniformly, i.e., \( d \ll (D t)^{1/2} \). The effective lifetime of Eq. (20) is plotted in Fig. 5 versus \( d \) as a function of \( s_r \).

For thin samples, \( \tau_{\text{eff}} \) no longer bears any resemblance to \( \tau_a \), the bulk lifetime and is dominated by surface recombination. The surface recombination velocity must be known to determine \( \tau_a \) unambiguously unless the sample is sufficiently thick. Although the surface recombination velocity of a sample is generally not known, by providing the sample with high \( s_r \), for example, it is possible to determine \( \tau_a \) directly. However, the sample must be extraordinarily thick. Equation (22) can be written as

\[ \frac{1}{\tau_{\text{eff}}} = \frac{1}{\tau_a} + \frac{1}{\tau_s} \]  

(23)

where \( \tau_s \) is the surface lifetime.

For \( s_r \to 0 \), a plot of \( 1/\tau_{\text{eff}} \) versus \( 1/d \) has a slope of \( 2s_r \) and an intercept of \( 1/\tau_a \), allowing both \( s_r \) and \( \tau_a \) to be determined. For \( s_r \to \infty \), a plot of \( 1/\tau_{\text{eff}} \) versus \( 1/d^2 \) has a slope of \( \pi^2 D \) and an intercept of \( 1/\tau_a \). Both equations are illustrated in Fig. 6. The approximation \( \tau_s = d/2s_r \) holds for \( s_r < D/4d \).

Equations (22)–(24) hold for samples with one dimension much smaller than the other two dimensions, for example, a wafer. For samples with none of the three dimensions very large, Eq. (23) becomes for \( s_r \to \infty \)

\[ \frac{1}{\tau_{\text{eff}}} = \frac{1}{\tau_a} + \pi^2 D \left( \frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} \right) \]  

(25)

where \( a, b \) and \( c \) are the sample dimensions. It is recommended that the sample surfaces have high surface recombination velocities. The recommended dimensions and the maximum bulk lifetimes that can be determined through Eq. (23) for Si samples are given in Table 2.

The approximation \( \tau_a = d/2s_r \) holds for \( s_r < D/4d \).

Two limiting cases are of particular interest: \( s_r \to 0 \) gives \( \tan(\beta d/2) = \beta d/2 \) and \( s_r \to \infty \) gives \( \tan(\beta d/2) = \infty \) or \( \beta d \approx \pi/2 \), making the surface lifetime

\[ \tau_s(s_r \to \infty) = \frac{d}{2s_r} \]  

(24)

1) Photoconductance Decay: The photoconductance decay lifetime characterization technique was proposed in 1955 [15] and has become one of the most common lifetime measurement techniques. As the name implies, ehps are created by optical excitation and their decay is monitored as a function of time following the cessation of the excitation. Other excitation means such as high-energy electrons and gamma rays can also be used. The samples may either be contactless (Fig. 7) or the measurement can be contacted with the current being monitored (Fig. 8).

![PCD measurement schematic for contactless (a) rf bridge and (b) microwave reflectance measurements](image_url)

![Schematic diagram for contact photoconductance decay measurement](image_url)
2) Quasi-Steady-State Photoconductance (QSSPC): In the QSSPC method the sample is illuminated with a flash lamp with a decay time constant of several ms and an illumination area of several cm$^2$\cite{7,9}. Due to the slow decay time, the sample is under quasi steady-state conditions during the measurement as the light intensity varies from its maximum to zero. The steady-state condition is maintained as long as the flash lamp time constant is longer than the effective carrier lifetime. The time-varying photoconductance is determined from the light intensity measured with a calibrated detector. The excess carrier density is calculated from the photoconductance signal. The generation rate, required in Eq. (7.25), is determined from the light intensity measured with a calibrated detector. Semiconductors absorb only a fraction of the incident photons, depending on the reflectivity of the front and back surfaces, possible faceting of those surfaces, and the thickness of the wafer. The value of the absorption fraction for a polished, bare silicon wafer is $f \approx 0.6$.

If the wafer has an optimized antireflection coating, $f \approx 0.9$, while a textured wafer with antireflection coating can approach $f \approx 1.36$ The generation rate per unit volume $G$ can then be evaluated from the incident photon flux and the wafer thickness, according to where is the photon flux density and the sample thickness. Assuming the flash lamp light decay is exponential in time, the generation rate is higher for $\tau_{\text{eff}} < \tau_{\text{flash}}$, the sample is in quasi steady-state during the measurement. Hence, the flash lamp decay time must be sufficiently long for the QSSCP measurement to be valid.

4. Conclusions

The microwave reflection or inductive coupling photoconductance decay technique is commonly used to measure carrier lifetime. Its key strength is the contactless nature and rapidness and major weakness is the unknown surface recombination velocity. If the sample thickness can be changed, then both the bulk lifetime and the surface recombination velocity can be extracted. The quasi-steady-state photoconductance method is a more recent method and has found wide acceptance in the design of photovoltaic devices. It measures the lifetime as a function of injection level in one step but requires large sample area (several cm$^2$) precluding high density mapping. Surface photovoltage technique is used to detect iron in $p$-Si. The most common electrical recombination lifetime method is the open-circuit voltage decay method. Measured $\tau_r$ or $L_n$ mean little for thin layers, e.g., epitaxial layers on highly doped substrates, denuded zones on heavily precipitated substrates, or SOI films. Such layers are best characterized through generation lifetime characterization \cite{16} which is commonly determined with the pulsed MOS capacitor. The Zerbst plot implementation is the most common, but the current versus reverse capacitance is easier to interpret because the doping density of the sample need not be known. Since $\tau_r$ is measured in the space-charge region of a reverse-biased device, it lends itself easily for the characterization of thin layers. Since the $scr$ width can be varied by an applied voltage, it is possible to generate a $\tau_r$ depth profile, that is difficult to do with $\tau_r$ measurements, because the measurement depth for $\tau_r$ and $L_n$ measurements is the minority carrier diffusion length.

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