

# Entropy Generation in a Plate-Fin Compact Heat Exchanger with Louvered Fins

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**Abstract** This study explores the generation of entropy in a plate-fin heat exchanger with Louvered fins. The objectives are finding the number of total entropy generation units under a given heat duty and pressure drop constraints. To clarify method, a heat exchanger for cooling water is designed. The overall assessment of cooling system requires a trade-off between thermal performance and pressure drop. Entropy generation minimization (EGM) method is based on the theory that a thermodynamically optimized system is the least irreversible, or minimum entropy generation in the system. At air side, ten types of fins are employed. Eventually, based on the entropy generation and thermal performance a type of fin is selected for designing. To optimize the performance of selected heat exchanger, an equation for finding optimal mass flow rate is offered. Using this optimal mass flow rate, the entropy generation decreased up to 21% and also energy consumption about 5%.

**Keywords** Entropy Generation, Plate-Fin Heat Exchanger, Louvered Fin

## 1. Introduction

Compact heat exchangers are used in a variety of automotive, residential air-conditioning, oil industry and refrigeration. For air-side heat transfer augmentation, louvered fin are quite popular. Beauvais[1] was the first to conduct flow visualization experiments on the louvered fin array. He demonstrated that louvers, rather than acting as surface roughness that enhanced heat transfer performance, acted to realign the airflow in the direction parallel to themselves. Davenport[2] performed flow visualization experiments identical to those of Beauvais and further demonstrated two flow regimes, duct directed flow, and louver directed flow.

Zhang et al. (1997) observed similar vortex shedding phenomena in a two-dimensional computational study. Inline and offset parallel plate models were created with periodic boundary conditions to simulate an infinite array in all directions, thus ignoring entrance and exit effects. It was determined that the vortex shedding served to increase the overall heat transfer of the louver. Unsteady solutions to the models showed that the vortices alternated shedding off the top and bottom of the plate and, correspondingly, had the effect of alternately increasing and decreasing the convective heat transfer along the plate surface. However, the time-averaged result of the vortices resulted in a smooth,

decreasing heat transfer curve from the leading edge to the trailing edge. This result disagrees with the DeJong et al. (1997) finding that showed a local heat transfer maximum at a location where the separated flow from the leading edge reattached to the plate at high Reynolds numbers. Both studies agreed, however, that the overall effect of vortex shedding was to increase the heat transfer in the array.

Kurosaki et al. (1988) studied the effects that thermal wakes have on the heat transfer of downstream louvers in various arrangements of parallel plates. Using laser holographic interferometry to visualize isothermal contours of the wakes off the back of the plates, they were able to observe the manner in which the wakes from upstream plates progressed downstream and interacted with downstream louvers. Thermal wake visualization showed that increasing the Reynolds number caused the wake to narrow and maintain form further downstream, in agreement with the data of Springer and Thole (1998a) and the predictions of Zhang et al. (1997). Heat transfer measurements on downstream plates indicated that direct interactions with wakes had an adverse effect on the convective heat transfer of the plates. By shifting the louvers such that they avoided the wakes of upstream plates for as long as possible, the heat transfer of the downstream louvers was increased due to the relatively cooler fluid surrounding the louvers. Additionally, increasing the streamwise distance between aligned louvers was shown to have a minimal effect on the heat transfer of the downstream louver except at high Reynolds numbers. At high Reynolds numbers, the difference in thickness between the thermal boundary layer on the upstream and downstream louver became more significant, causing decreased heat

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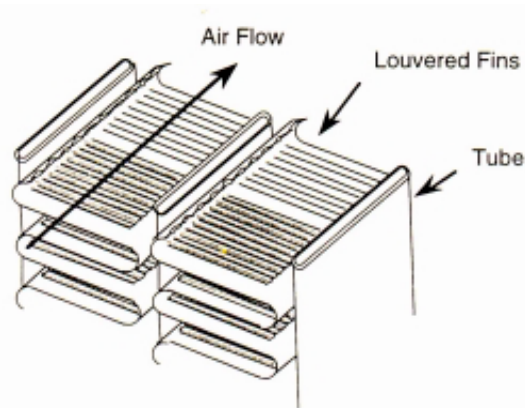
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Published online at <http://journal.sapub.org/ijee>

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transfer performance on the downstream louver as compared to the upstream louver.

| Nomenclature                      |                                      |
|-----------------------------------|--------------------------------------|
| $A_f$ : fin area                  | Nu : Nusselt number                  |
| $A_p$ : primary area              | NTU : number of transfer unit        |
| $A_t$ : heat transfer area        | $n_f$ : total number of fins         |
| b: tube spacing                   | $n_{louv}$ : total number of louvers |
| $C_p$ : specific heat             | $P_f$ : fin pitch                    |
| $D_h$ : hydraulic diameter        | $P_l$ : Louver pitch                 |
| f: friction factor                | P: pressure                          |
| h: convective coefficient         | $q'$ : heat transfer per unit length |
| $H_t$ : tube height               | Re : Reynolds number                 |
| j: Colburn factor                 | St : Stanton number                  |
| $K_C$ : Contraction coefficient   | $S_{gen}$ : entropy generation       |
| $K_e$ : expansion coefficient     | T : temperature of fluids            |
| $K$ : thermal conductivity        | $W_t$ : tube outside pitch           |
| $L_{louv}$ : louver cut length    | Greek symbols                        |
| $L_p$ : louver pitch              | $\rho$ : fluid density               |
| $\dot{m}$ : mass flow rate        | $\mu$ : dynamic viscosity            |
| $N_{pg}$ : number of passages     | Subscripts                           |
| $N_s$ : entropy generation number | 1 : Water                            |
| $N_t$ : total number of tubes     | 2 : Air                              |



**Figure 1.** Schematic of a typical louvered fin-and-tube heat exchanger

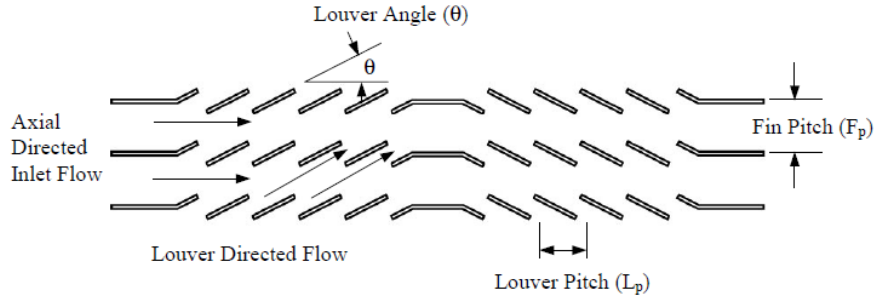


Figure 2. Side view of a typical louvered fin geometry

## 2. Thermal-hydraulic Design

In the thermal design of heat exchangers, two of the most important problems involve rating and sizing. Determination of heat transfer and pressure drop is referred to as rating problem. Determination of a physical size such as length, width, height, and surface area on each side is referred to as a sizing problem. When the heat transfer rate is not known or the outlet temperature are not known, tedious iterations with the LMTD method are required. In an attempt to eliminate the iterations, Kays and London in 1995 developed a new method called the  $\varepsilon$ -NTU method. Here, the heat capacity rate is defined as the product of mass flow rate and specific heat. The minimum capacity rate is the one that has a lesser capacity rate, and the maximum capacity rate is then the one that has a higher capacity rate. So, the heat transfer rate is,

$$Q = \varepsilon C_{\min} (T_{h,i} - T_{c,i}) = \varepsilon C_{\min} \Delta T_{\max} \quad (1)$$

Here  $\varepsilon$ ,  $\Delta T_{\max}$  and  $C_{\min}$  are the heat exchanger efficiency, entering temperature difference and the minimum of heat capacity respectively.

$$\varepsilon = 1 - \exp\left\{\left(\frac{1}{C^*}\right) NTU^{0.22} \left[\exp(-C^* \cdot NTU^{0.78}) - 1\right]\right\} \quad (2)$$

Where  $C^*$  is defined by:

$$C^* = \frac{C_{\min}}{C_{\max}} = \frac{(\dot{m}C_p)_{\min}}{(\dot{m}C_p)_{\max}} = \begin{cases} \frac{(T_{c,o} - T_{c,i})}{(T_{h,i} - T_{h,o})} & \text{for } C_h = C_{\min} \\ \frac{(T_{h,i} - T_{h,o})}{(T_{c,o} - T_{c,i})} & \text{for } C_c = C_{\min} \end{cases} \quad (3)$$

The other important parameter is NTU, Where it is considered as the number of transfer unit.

$$NTU = \frac{UA}{C_{\min}} = \frac{1}{C_{\min}} \int_A U dA \quad (4)$$

To calculate the outlet temperatures of both fluids, hot and cold, the equation of (5) and (6) can be considered.

$$T_{h,o} = T_{h,i} - \varepsilon \left(\frac{C_{\min}}{C_h}\right) \cdot (T_{h,i} - T_{c,i}) \quad (5-a)$$

$$T_{c,o} = T_{c,i} + \varepsilon \left(\frac{C_{\min}}{C_c}\right) \cdot (T_{h,i} - T_{c,i}) \quad (5-b)$$

One of the key stage in designing a heat exchanger is accurate calculation of fluid properties. But before doing this, it is necessary to compute average temperature of each fluid.

Here, according to shah research, if  $C^* \geq 0.50$  the average temperatures would be

$$T_{h,m} = \frac{T_{h,i} + T_{h,o}}{2} \quad (6-a)$$

$$T_{c,m} = \frac{T_{c,i} + T_{c,o}}{2} \quad (6-b)$$

Heat transfer coefficient is,

$$h = j \cdot G \cdot C_p \cdot Pr^{\frac{-2}{3}} \quad (7)$$

$$G = \frac{\dot{m}}{A_{fr}} \quad (8)$$

In this formula,  $G$  and  $A_{fr}$  are mass velocity and free flow cross sectional area respectively. Also, Colburn factor is,

$$j = Re^{-0.49} \left(\frac{\theta}{90}\right)^{0.27} \left(\frac{P_f}{L_p}\right)^{-0.14} \left(\frac{b}{L_p}\right)^{-0.29} \left(\frac{W_t}{L_p}\right)^{-0.23} \\ \times \left(\frac{L_{low}}{L_p}\right)^{0.68} \left(\frac{P_t}{L_p}\right)^{-0.28} \left(\frac{\delta}{L_p}\right)^{-0.05} \quad (9)$$

Where  $L_p$  is the louver pitch,  $\theta$  the louver angle,  $P_f$  the fin pitch,  $P_t$  the tube pitch,  $b$  the tube spacing,  $W_t$  the tube outside width,  $L_{low}$  the louver cut length, and  $\delta$  the fin thickness. Furthermore, frictional pressure drop in both sides is given by:

$$\Delta P_1 = \frac{G_1^2}{2\rho_{in,1}} \left[ \left(1 + K_{c,1} - \sigma_1^2\right) + 2 \left(\frac{\rho_{in,1}}{\rho_{out,1}} - 1\right) + \left(f_1 \times \frac{S_1}{A_1} \times \frac{\rho_{in,1}}{\rho_{m,1}}\right) \right] \\ - \left(1 - \sigma_1^2 - k_{e,1}\right) \times \frac{\rho_{in,1}}{\rho_{out,1}} \quad (10)$$

Here  $K_c$  and  $K_e$  are contraction and expansion coefficients.

The noncircular diameter in the flow channels are approximated using the hydraulic diameter for the Reynolds number. The hydraulic diameter is defined as,

$$D_h = \frac{4A_c}{P_{wetted}}$$

Where  $N_t = N_{pg} + 1$  is the wetted perimeter. The thermal design of a heat exchanger is aimed at calculating a surface area adequate to handle the thermal duty for the given

specifications. Fluid friction effects in the heat exchanger are important because they determine the pressure drop of the fluids flowing in the system, and consequently the pumping power or fan work input necessary to maintain the flow.

The number of passages  $N_{pg}$  on the hot side is defined as the air flow passages between flat tubes. The core width  $L_1$  is expressed in terms of the number of passages  $N_{pg}$  as

$$L_1 = N_{pg}b + (N_{pg} + 1)H_t \quad (11)$$

Where  $b$  is the tube spacing and  $H_t$  the tube height. Solving for the number of passages  $N_{pg}$  gives

$$N_{pg} = \frac{L_1 - H_t}{b + H_t} \quad (12)$$

The total number of fins is

$$n_f = \frac{L_3}{P_f} N_{pg} \quad (13)$$

The total heat transfer area  $A_t$  is generally obtained from the sum of the primary area  $A_p$  and the fin area  $A_f$ . The primary area  $A_p$  is calculated by subtracting the fin base areas from the tube outer surface areas, considering the circular front and end of the tubes.

$$A_p = [2(L_2 - H_t) + \pi H_t] L_3 (N_{pg} + 1) - 2\delta L_2 n_f \quad (14)$$

The total number of louvers in the core is obtained as

$$n_{louv} = \left( \frac{L_f}{L_p} - 1 \right) n_f \quad (15)$$

So, the total fin area is the sum of the fin area and the louver edge area as

$$A_f = 2(s_f L_2 + s_f \delta) n_f + 2L_{louv} \delta n_{louv} \quad (16)$$

Here  $s_f$  is the fin width. The total heat transfer area is,

$$A_{t1} = [2(L_2 - H_t) + \pi(H_t - 2\delta_w)] L_3 N_t \quad (17)$$

The minimum free-flow area  $A_{c2}$  is expressed by:

$$A_{c2} = bL_3 N_{pg} - [\delta(\delta_f - L_{louv}) + L_{louv} \cdot L_h] n_f \quad (18)$$

In coolant side, the total number of tubes is,

$$N_t = N_{pg} + 1 \quad (19)$$

Considering the circular shapes at both ends, the total heat transfer area  $A_{t1}$  on the coolant side is obtained by,

$$A_{t1} = [2(L_2 - H_t) + \pi(H_t - 2\delta_w)] L_3 N_t \quad (20)$$

The free-flow area  $A_{c1}$  on the coolant side is:

$$A_{c1} = \left[ (L_2 - H_t)(H_t - 2\delta_w) + \frac{\pi}{4}(H_t - 2\delta_w)^2 \right] \frac{N_t}{N_p} \quad (21)$$

### 3. Entropy Generation

In a large number of convective heat transfer situations the velocity and temperature fields are not known at each point in the medium. This is a case when the flow regime is

turbulent or when the flow geometry is so complicated that an exact description of velocity and temperature is not available in analytical or numerical form.

Consider the flow passage of arbitrary cross-section "A" and wetted perimeter "P". The bulk properties of the stream  $\dot{m}$  are  $T, P, H, S, \rho$ . In general, this heat transfer arrangement is characterized by a finite frictional pressure gradient  $-dP/dX > 0$  and when heat is transferred to the stream at a rate  $q'(W/m)$ , by a finite wall-bulk fluid temperature difference  $\Delta T$ . Focusing on a slice of thickness  $dx$  as a system, the rate of entropy generation is given by the second law:

$$d\dot{S}_{gen} = \dot{m}ds - \frac{q'dx}{T + \Delta T} \quad (22)$$

In addition, for any pure substance we write the canonical relation as:

$$\frac{dh}{dx} = T \frac{ds}{dx} + \frac{1}{\rho} \frac{dP}{dx} \quad (23)$$

This formula can be related to average heat transfer and fluid friction information, which may be obtained experimentally or numerically for most duct geometries. The relationship between heat transfer rate  $q'$  and wall-bulk fluid temperature difference is expressed in the form of Stanton number correlations:

$$St = \frac{q' / P \Delta T}{C_p G} \quad (24)$$

Here, note is that  $q' / P \Delta T$  is the average heat transfer coefficient. The fluid friction characteristics of a certain duct are reported usually in the form of friction factor correlations:

$$f = \frac{\rho D}{2G^2} \left( -\frac{dP}{dx} \right) \quad (25)$$

In order to illustrate the dependence of  $\dot{S}_{gen}$  on Stanton number and friction factor information, we consider the case in which the heat transfer rate per unit length  $q'$  and the mass flow rate  $\dot{m}$  are specified. So,

$$\dot{S}_{gen} = \frac{q'^2}{4T^2 \dot{m} C_p} \frac{D}{St} + \frac{2\dot{m}^3}{\rho^2 T} \frac{f}{DA^2} \quad (26)$$

Under the present assumptions the duct configuration has two degrees of freedom. The wetted perimeter  $P$  and the cross-sectional area  $A$  or any other couple of independent parameters such as  $(Re, D)$  or  $(G, D)$ .

Examining this Equation, it becomes evident that a high Stanton number contributes to the reduction of heat transfer share of  $\dot{S}_{gen}$ , while a high friction factor has the effect of increasing the entropy generation rate due to viscous effects.

In a round tube of diameter  $D$ , the rate of entropy generation per unit length is:

$$\dot{S}_{gen} = \frac{q'^2}{\pi k T^2 Nu} + \frac{32\dot{m}^3}{\pi^2 \rho^2 T D^5} f \quad (27)$$

Here, the Nusselt number is  $Nu = St \cdot Re \cdot Pr$ . If the pipe flow

is turbulent and fully developed, the Nusselt number and friction factor are given by the well-known correlations (e.g., Bejan, 1995):

$$Nu = 0.023 Re^{0.8} Pr^{0.4} \quad (28)$$

$$f = 0.046 Re^{-0.2} \quad (29)$$

If  $\tau = \Delta T / T$ , in louver fins side the number of entropy generation is:

$$N_s = \frac{\tau}{1 + \tau} + \frac{J^2 f Re^2}{32 St^3 \tau^3} \quad (30)$$

Where  $J$  and  $N_s$  are respectively,

$$J = \frac{\mu q'}{\rho \dot{m} (C_p T)^{1.5}} \quad (31)$$

$$N_s = \frac{S'_{gen}}{q' / T} \quad (32)$$

## 4. A case study

A coolant to air cross flow heat exchanger is design to cool the coolant (50 percent ethylene glycol with water). Louvered fin geometry is employed on the air side. Both fins and tubes are made from aluminum alloy with  $K = 117 W / mK$ . The coolant flow in the flat tubes at  $1.65 \times 10^{-3} m^3 / s$  and  $95 C^\circ$ , and shall leave at  $90 C^\circ$ . Air enters at  $1.05 m^3 / s$  and  $25 C^\circ$ . The inlet pressure of the air is at  $100 Kpa$  absolute and the inlet pressure of the coolant is at  $200 Kpa$  absolute. The air pressure drop is required to be less than  $500 Pa$ . The coolant pressure drop is recommended to be less than  $70 Kpa$ .

**Table 1.** Fin geometries

|    | Surface designation | Plate spacing<br>( $10^{-3} m$ ) | Hydraulic diameter<br>( $10^{-3} m$ ) | Fin thickness<br>( $10^{-3} m$ ) | Louver spacing<br>( $10^{-3} m$ ) | Louver gap<br>( $10^{-3} m$ ) | Heat transfer area/volume between plate<br>( $m^2 / m^3$ ) | Fin area/total area |
|----|---------------------|----------------------------------|---------------------------------------|----------------------------------|-----------------------------------|-------------------------------|--|---------------------|
| 1  | 3/8-6.06            | 6.35                             | 4.453                                 | 0.152                            | 9.525                             | 1.397                         | 840  | 0.640               |
| 2  | 3/8(a)-6.06         | 6.35                             | 4.453                                 | 0.152                            | 9.525                             | 3.302                         | 840  | 0.640               |
| 3  | 1/2-6.06            | 6.35                             | 4.453                                 | 0.152                            | 12.70                             | 1.397                         | 840  | 0.640               |
| 4  | 1/2(a)-6.06         | 6.35                             | 4.453                                 | 0.152                            | 12.70                             | 3.302                         | 840  | 0.640               |
| 5  | 3/8-8.7             | 6.35                             | 3.650                                 | 0.152                            | 9.525                             | 1.397                         | 1007   | 0.705               |
| 6  | 3/8(a)-8.7          | 6.35                             | 3.650                                 | 0.152                            | 9.525                             | 2.032                         | 1007   | 0.705               |
| 7  | 3/16-11.1           | 6.35                             | 3.084                                 | 0.152                            | 4.763                             | 1.397                         | 1204   | 0.756               |
| 8  | 1/4-11.1            | 6.35                             | 3.084                                 | 0.152                            | 6.350                             | 1.397                         | 1204   | 0.756               |
| 9  | ¼(b)-11.1           | 6.35                             | 3.084                                 | 0.152                            | 6.350                             | 1.397                         | 1204   | 0.756               |
| 10 | 3/8-11.1            | 6.35                             | 3.084                                 | 0.152                            | 9.525                             | 1.397                         | 1204   | 0.756               |

## 5. Results and Discussions

Table 2 denotes the fluid properties. At this stage ten heat exchangers with different Louvered fins are designed and compared for different terms. Table 3 gives this information.

**Table 2.** Fluid properties

|       | $\rho (kg / m^3)$ | $C_p (J / Kg.K)$ | $K (W / m.K)$ | $\mu (N.S / m^2)$     | Pr    |
|-------|-------------------|------------------|---------------|-----------------------|-------|
| Water | 1020              | 3650             | 0.442         | $8 \times 10^{-4}$    | 6.6   |
| Air   | 1.168             | 1007             | 0.022         | $1.84 \times 10^{-5}$ | 0.707 |

In tube side, with decreasing hydraulic diameter heat transfer and pressure drop characteristics will increase. However, the difference is not very considerable. For example, from 3/8-6.06 fin with hydraulic diameter of 4.453 millimetre to 3/8-11.1 fin with hydraulic diameter of 3.084 millimetre the increase in pressure drop is just  $1 Kpa$ . For heat transfer coefficient and Reynolds number is the same. However, in Air side there is considerable difference between different type of fins. The important note is that Reynolds number, here, is a function of Louver gap and Louver spacing.

$$Re = f(\text{Louver gap}, \text{Louver spacing}) \quad (33)$$

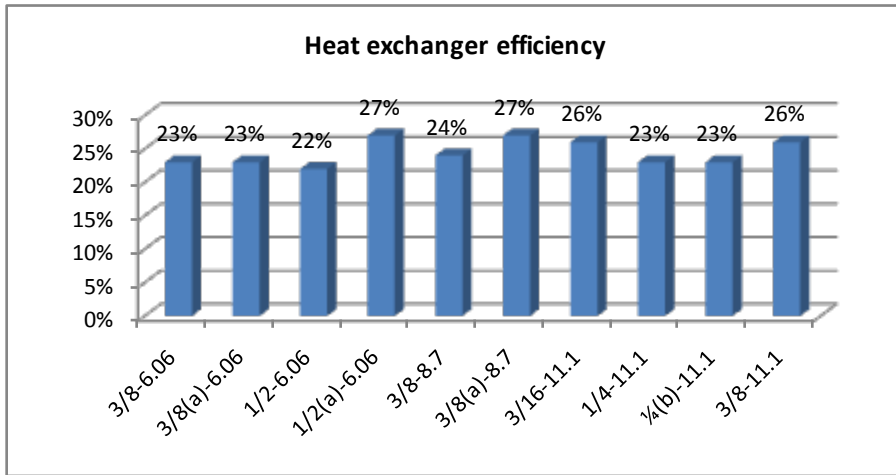
Fins of 3/8(a)-6.06 and 1/2(a)-6.06 have the biggest Louver gap, but between them the fin of 1/2(a)-6.06 with 12.70 millimetre Louver spacing has the highest value of Reynolds number. Among cases of 1, 3, 5, 7, 8, 9 and 10 with the same Louver gap, the fin of 1/2-6.06 has the highest Reynolds number. For the convective coefficient and mass velocity the trend is the same as Reynolds number.

**Table 3.** Designing information

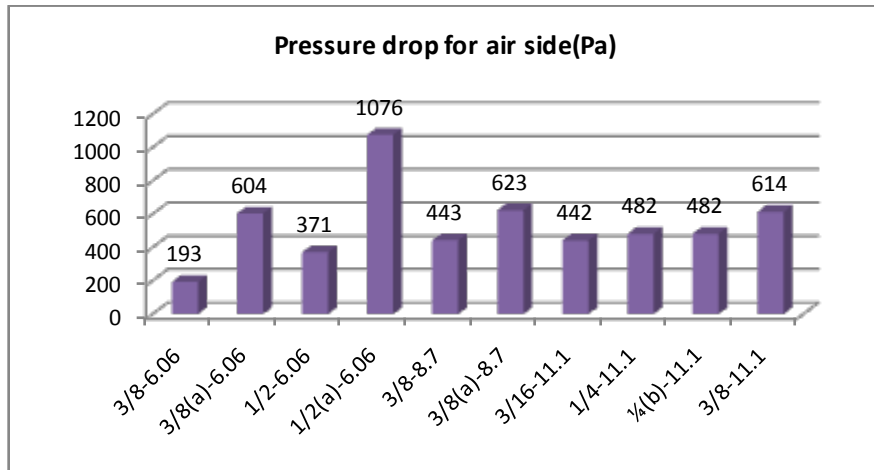
|                    | 1                     | 2                     | 3                     | 4                     | 5                     | 6                     | 7                     | 8                     | 9                     | 10                    |
|--------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|
| $n_f$              | 4359                  | 4359                  | 4359                  | 4359                  | 6269                  | 6269                  | 8255                  | 8255                  | 8255                  | 8255                  |
| $A_p(m^2)$         | 1.23                  | 1.23                  | 1.23                  | 1.23                  | 1.21                  | 1.21                  | 1.19                  | 1.19                  | 1.19                  | 1.19                  |
| $A_f(m^2)$         | 2.504                 | 2.330                 | 2.60                  | 2.368                 | 3.650                 | 3.51                  | 4.469                 | 4.560                 | 4.560                 | 4.742                 |
| $A_{t,1}(m^2)$     | 1.238                 | 1.238                 | 1.238                 | 1.238                 | 1.238                 | 1.238                 | 1.238                 | 1.238                 | 1.238                 | 1.238                 |
| $A_{c,1}(m^2)$     | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ | $1.13 \times 10^{-3}$ |
| $A_{t,2}(m^2)$     | 3.73                  | 3.560                 | 3.83                  | 3.598                 | 4.86                  | 4.72                  | 5.659                 | 5.75                  | 5.75                  | 5.932                 |
| $A_{c,2}(m^2)$     | 0.097                 | 0.070                 | 0.092                 | 0.056                 | 0.088                 | 0.075                 | 0.092                 | 0.088                 | 0.088                 | 0.079                 |
| $A_{fr,2}(m^2)$    | 0.153                 | 0.153                 | 0.153                 | 0.153                 | 0.153                 | 0.153                 | 0.153                 | 0.153                 | 0.153                 | 0.153                 |
| $G_1(kg/m^2.s)$    | 1489.3                | 1489.3                | 1489.3                | 1489.3                | 1489.3                | 1489.3                | 1489.3                | 1489.3                | 1489.3                | 1489.3                |
| $G_2(kg/m^2.s)$    | 12.64                 | 17.52                 | 13.33                 | 21.91                 | 13.94                 | 16.36                 | 13.33                 | 13.94                 | 13.94                 | 15.53                 |
| $Re_1$             | 8289                  | 8289                  | 8289                  | 8289                  | 6794                  | 6794                  | 5741                  | 5741                  | 5741                  | 5741                  |
| $Re_2$             | 3049                  | 4226                  | 3215                  | 5285                  | 2756                  | 3234                  | 2226                  | 2328                  | 2328                  | 2594                  |
| $h_1(W/m^2.K)$     | 6112                  | 6112                  | 6112                  | 6112                  | 6154                  | 6154                  | 6139                  | 6139                  | 6139                  | 6139                  |
| $h_2(W/m^2.K)$     | 160.1                 | 221.8                 | 168.8                 | 277.38                | 176.56                | 207.1                 | 168.75                | 176.48                | 176.48                | 196.6                 |
| $\eta_f$           | 0.92                  | 0.89                  | 0.91                  | 0.87                  | 0.91                  | 0.90                  | 0.91                  | 0.91                  | 0.91                  | 0.90                  |
| $\eta_o$           | 0.94                  | 0.92                  | 0.93                  | 0.91                  | 0.93                  | 0.92                  | 0.92                  | 0.92                  | 0.92                  | 0.92                  |
| $UA$               | 345.87                | 371.4                 | 335.3                 | 412.8                 | 390.56                | 412.3                 | 407.28                | 375.91                | 375.91                | 403.03                |
| $\varepsilon$      | 23%                   | 23%                   | 22%                   | 27%                   | 24%                   | 27%                   | 26%                   | 23%                   | 23%                   | 26%                   |
| $T_{1,O}(C^\circ)$ | 91.78                 | 91.78                 | 91.92                 | 91.22                 | 91.64                 | 91.22                 | 91.36                 | 91.78                 | 91.78                 | 91.36                 |
| $T_{2,O}(C^\circ)$ | 41.1                  | 41.1                  | 40.4                  | 43.9                  | 41.8                  | 43.9                  | 43.2                  | 41.1                  | 41.1                  | 43.2                  |
| $\Delta P_1(Kpa)$  | 22                    | 22                    | 22                    | 22                    | 22.5                  | 22.5                  | 23                    | 23                    | 23                    | 23                    |
| $\Delta P_2(Kpa)$  | 0.193                 | 0.604                 | 0.371                 | 1.076                 | 0.443                 | 0.623                 | 0.442                 | 0.482                 | 0.482                 | 0.614                 |

**Table 4.** Entropy generation

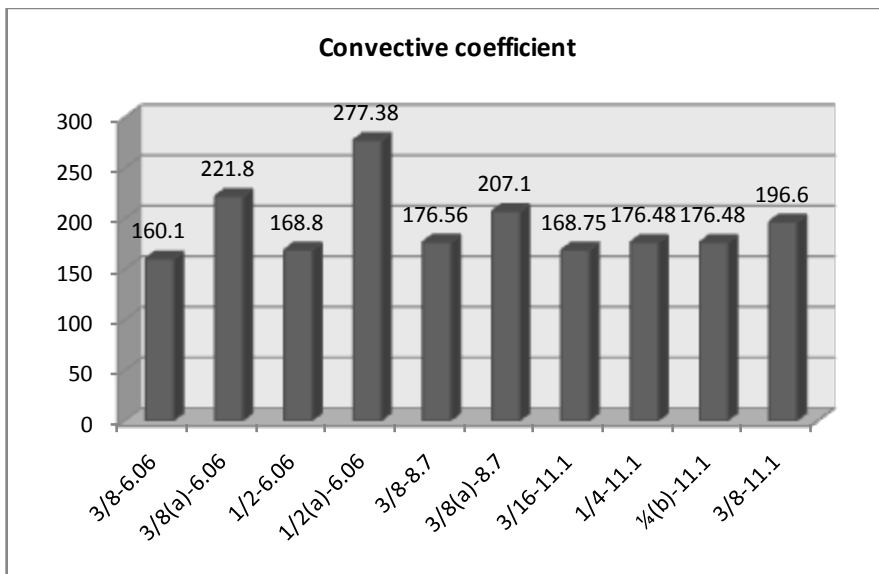
|              | 1      | 2      | 3      | 4     | 5      | 6     | 7      | 8      | 9      | 10     |
|--------------|--------|--------|--------|-------|--------|-------|--------|--------|--------|--------|
| <b>Water</b> | 110.73 | 110.73 | 110.50 | 111.1 | 110.93 | 111.1 | 111.03 | 110.73 | 110.73 | 111.03 |
| <b>Air</b>   | 20.80  | 20.81  | 19.29  | 26.59 | 22.36  | 26.47 | 24.97  | 20.53  | 20.53  | 26.81  |



**Figure 3.** Heat exchanger efficiency



**Figure 4.** Pressure drop for Air



**Figure 5.** Convective coefficient for Air

Here, allowable pressure drop for Air side is  $500 Pa$  , so the case of 7 is suitable, because it has the highest heat exchanger efficiency between all cases with allowable pressure drop. Table 4 gives entropy generation for Water and Air side. It is evident that entropy generation has a direct relation with heat exchanger efficiency , as in the case of 6 with the heat exchanger efficiency of 27% there are the largest value entropy generation in both sides. As previously mentioned , the selected fin for our designing is case of 7. However, here, the entropy generation is high and it is necessary decreasing it. To reach the optimal entropy generation in this case , we can change the mass flow rate. Equation of (34) demonstrates the optimal mass flow rate based on entropy minimization.

$$\left\{ \begin{array}{l} \dot{m}_{opt} = \frac{Re^2 D^2 \pi^2}{32q'^2} \quad \text{For Air side} \\ \dot{m}_{opt} = \frac{q'^2 \rho^2 D^5 \pi}{96 f T k Nu} \quad \text{For Water side} \end{array} \right. \quad (34)$$

Figures of (6) and (7) show the function of optimal mass flow rate for Water and Air side respectively. As it is clear from these Figures the optimal mass flow rate will increase with growing hydraulic diameter dramatically. However, in tube side this increase is more. In tube side, some factors such as Louver angle, Louver spacing and Louver gap are also determinant. Using equation of (34) the optimal mass flow rate for Water and Air are  $0.327$  and  $1.45 kg/s$  respectively. After doing mechanical and thermal designing process heat exchanger efficiency increased 5% and entropy generation decreased about 13.5% and 21 % for tube and fin side respectively.

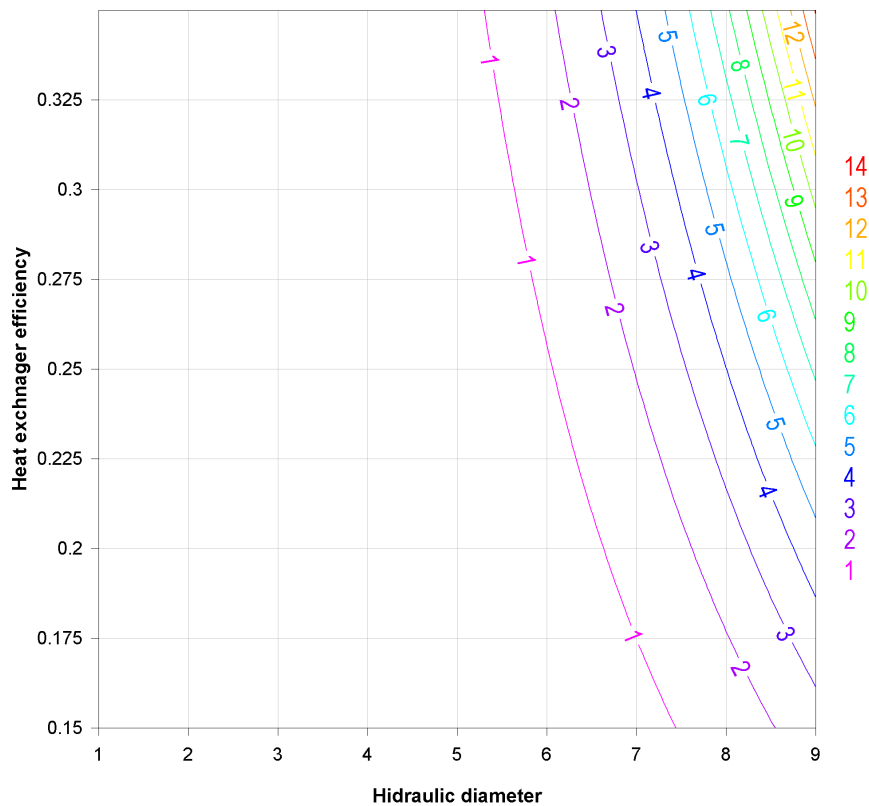


Figure 6. Optimal mass flow rate for Water based on entropy minimization



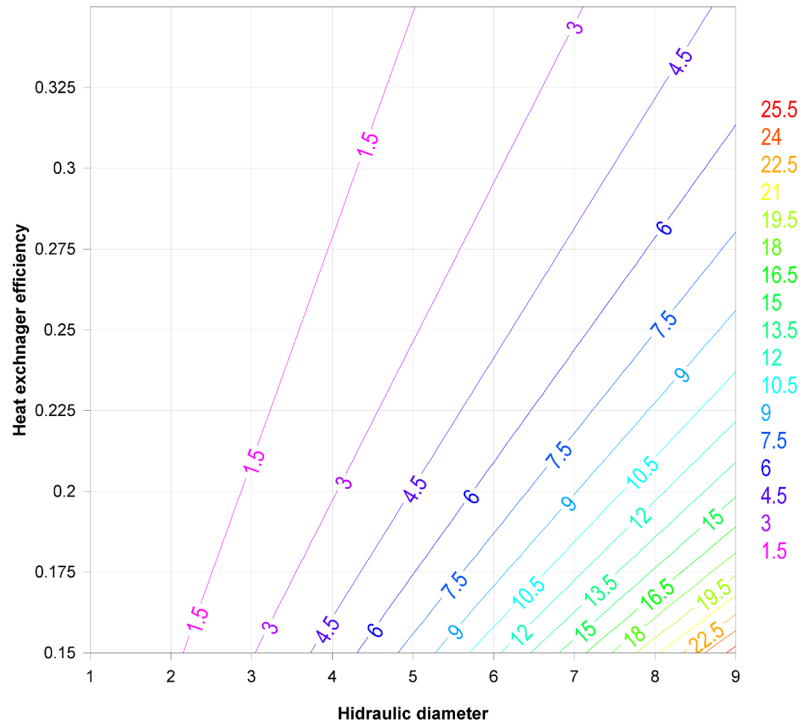


Figure 7. Optimal mass flow rate for Air based on entropy minimization

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